

Locomotion of Animals, Design of Robots and Mathematics



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Amazing Creature - True Slime Mold



Physarum Polycephalum

(和名：モジホコリ)

Large single cell organism
with multi nuclei

Tubular structure

Physarum can solve a maze !



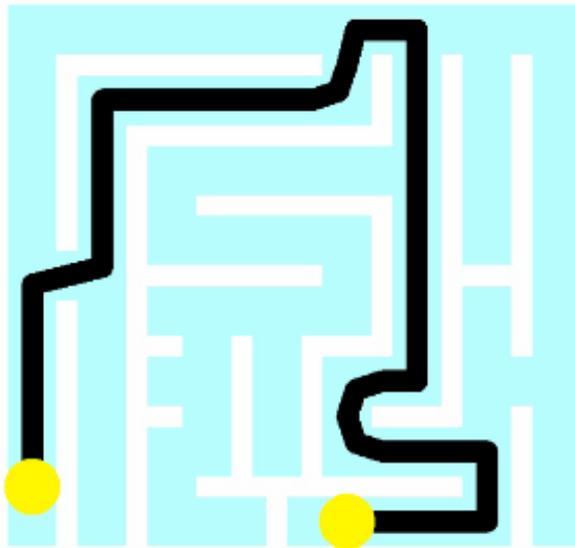
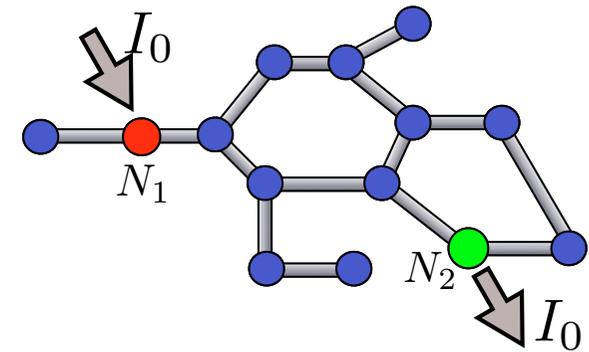
Nakagaki et al., Nature (2000)

Physarum Solver

Shortest path finding model on the graph

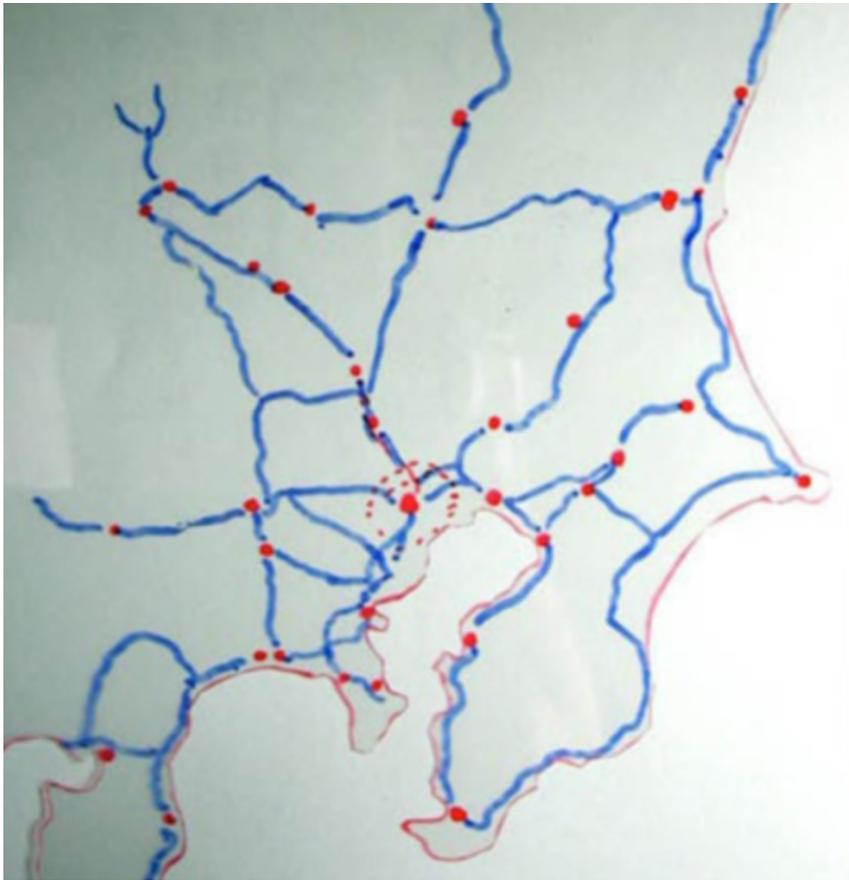
$$\sum_i \frac{D_{ij}}{L_{ij}} (p_i - p_j) = \begin{cases} -I_0 & \text{for } j = 1, \\ I_0 & \text{for } j = 2, \\ 0 & \text{otherwise.} \end{cases}$$

$$\frac{d}{dt} D_{ij} = f(|Q_{ij}|) - D_{ij} \quad Q_{ij} = \frac{D_{ij}}{L_{ij}} (p_i - p_j)$$

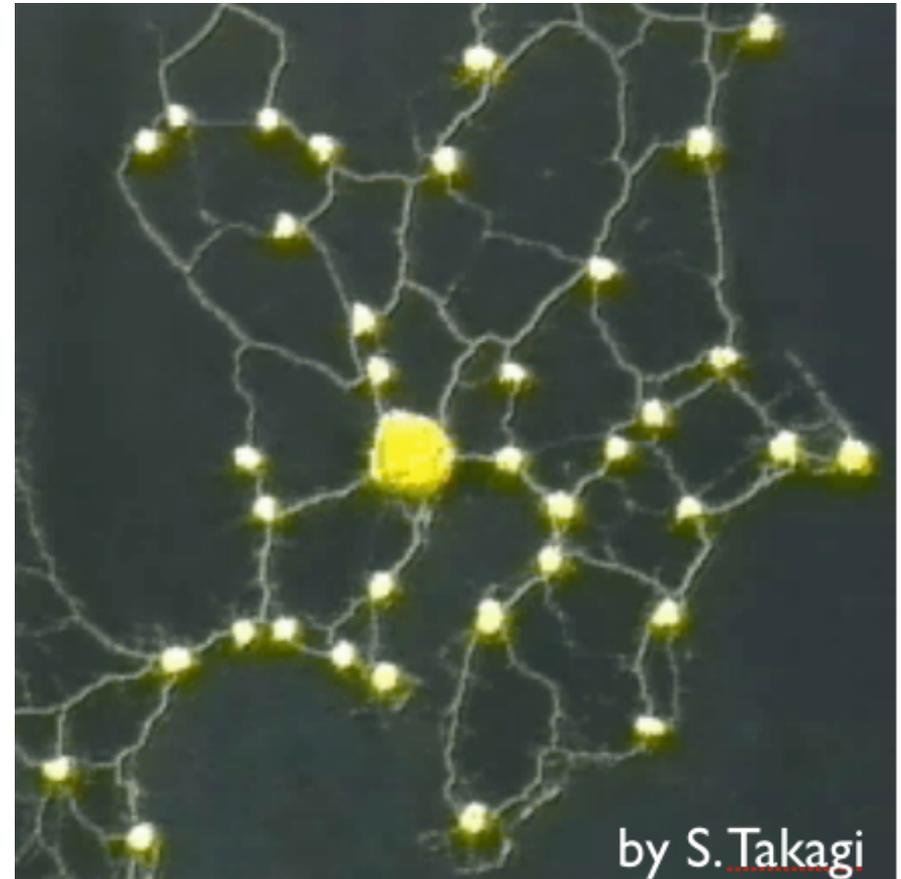


Physarum designs networks !

Real Railroad Network
in Tokyo area



Network produced
by *Physarum*



Efficiency ↔ Cost ↔ Fault tolerance

Tero et al., Science(2010)

Extended Physarum Solver

Cost



Efficiency, Fault tolerance



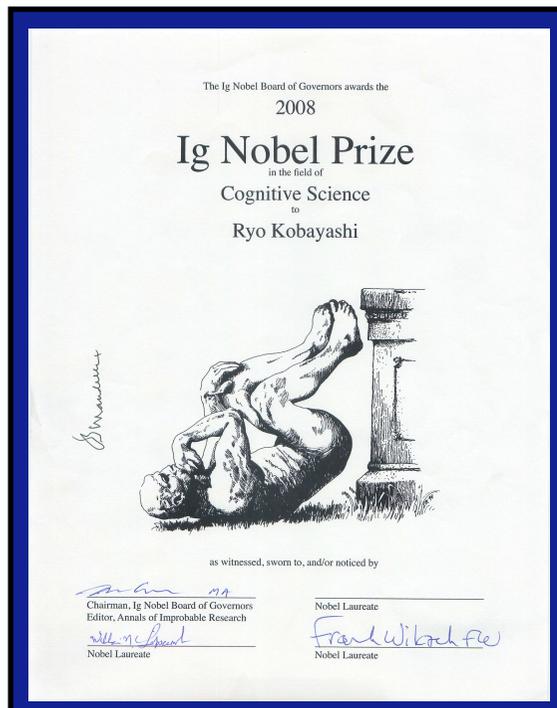
by A.Tero

Physarum is completely decentralized system !

Ig Nobel Prize

2008 Cognitive Science Prize

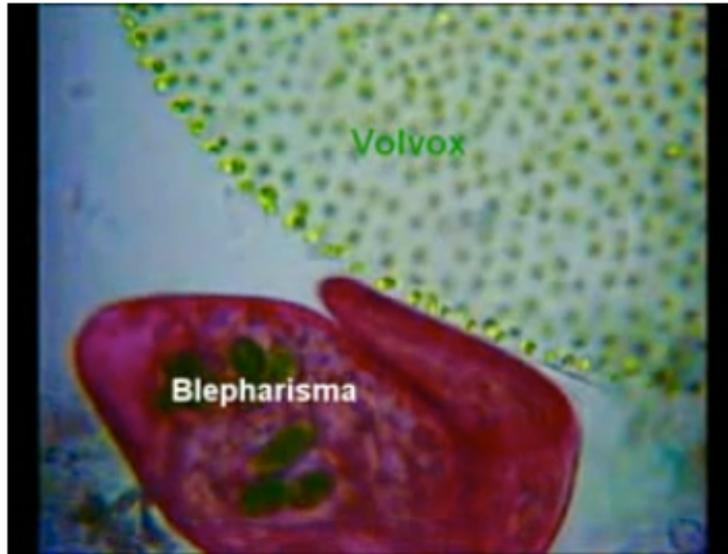
2010 Transportation Planning Prize



First make people laugh,
and then make them think



Locomotion of Animals



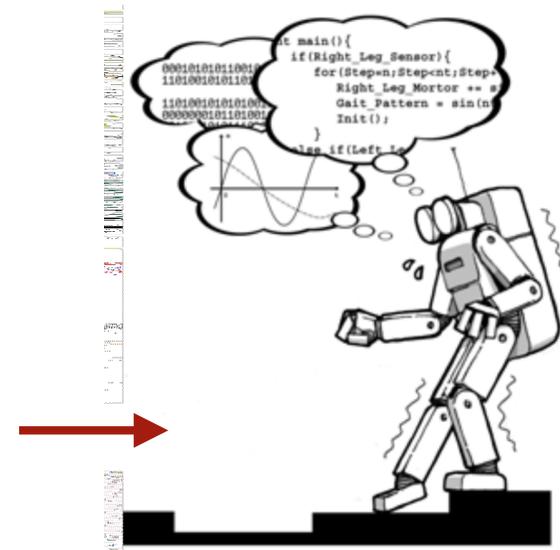
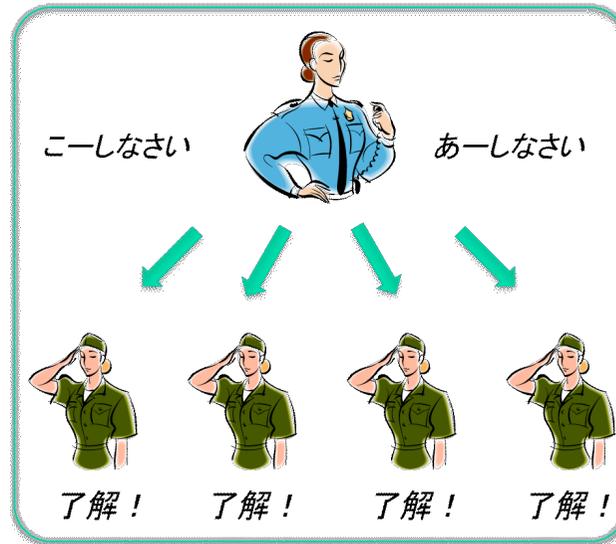
Supple, agile, robust motion

Control very large
degrees of freedom

Tough under uncertain
surroundings



Locomotion of Robots



Completely centralized control

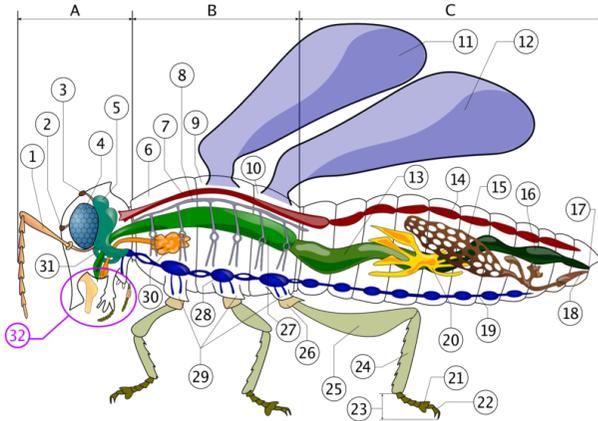


Decentralization

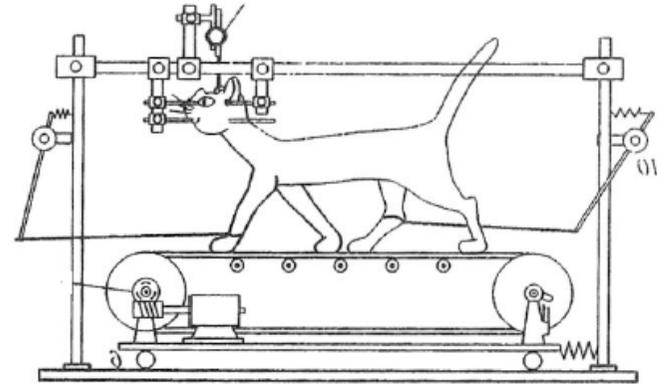
Autonomous Decentralized Control

Control policy which attains useful functions by the interactions between local elements having simple ability of sense, judge and motor output

ADC in Animals



Neural ganglion in each body segment



Gait transition of DC cat on treadmill

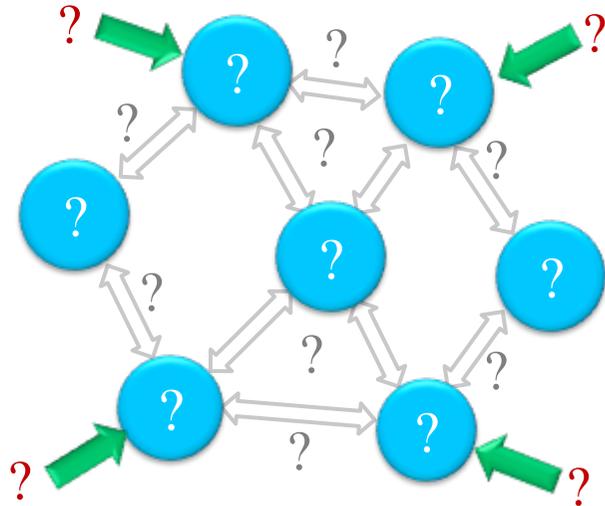
Central Pattern Generator

Neural circuits which generate rhythm

Lamprey, Tadpole ↔ Mammals

Details are still unknown

ADC is OK, but



How can we achieve the emergence of function from such systems ?

1. Dynamics of each component
2. Interaction between components
3. Local sensory feedback

ad hoc design for each case example

Still missing a systematic way of designing ADC !

Outline of Our Project

- Goal

Understand the animal's locomotion from the view point of mechanics and control

Produce robots which move in supple, agile and robust manner like animals

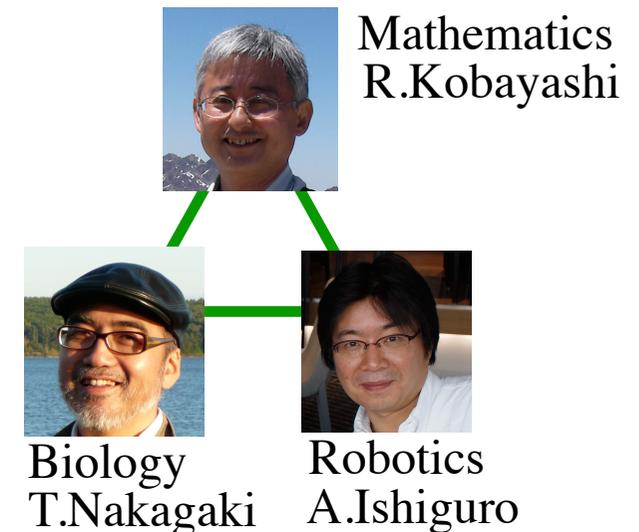
- Who ?

Team consists of Biologists, Mathematicians & Roboticists

- How ?

Learn from the animals

Design robots with large DOF controlled by ADC



Which animal at first ?

Go Back to *Physarum* !



Completely decentralized system

Driven by distributed oscillator system

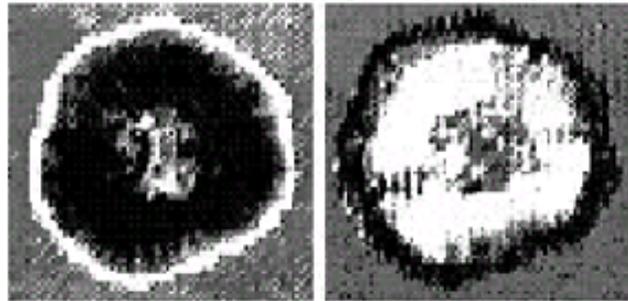
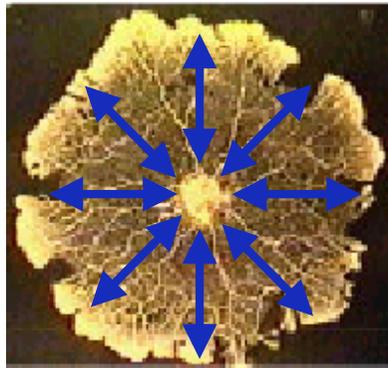
High ability

Solving a maze and designing networks

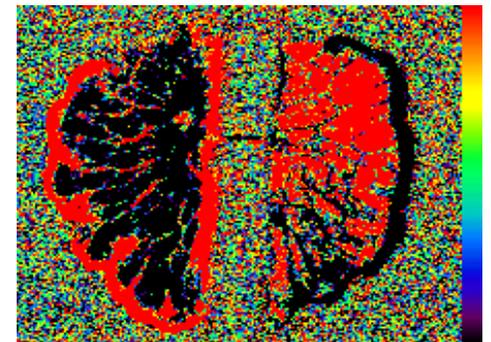
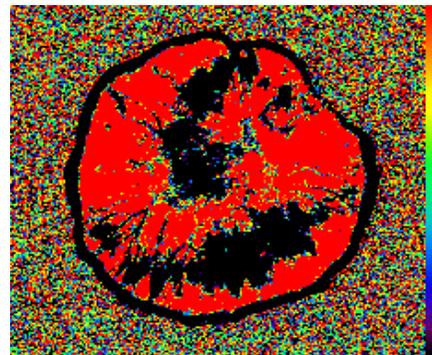
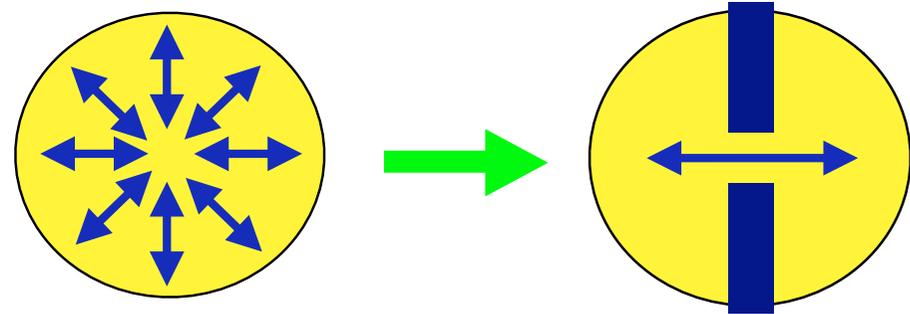


Anti-phase Oscillations

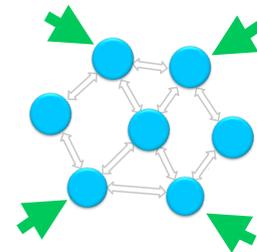
Peripheral Phase Inversion



Bottleneck Phase Inversion

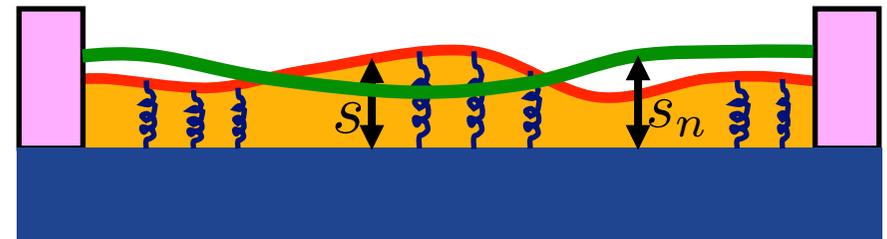
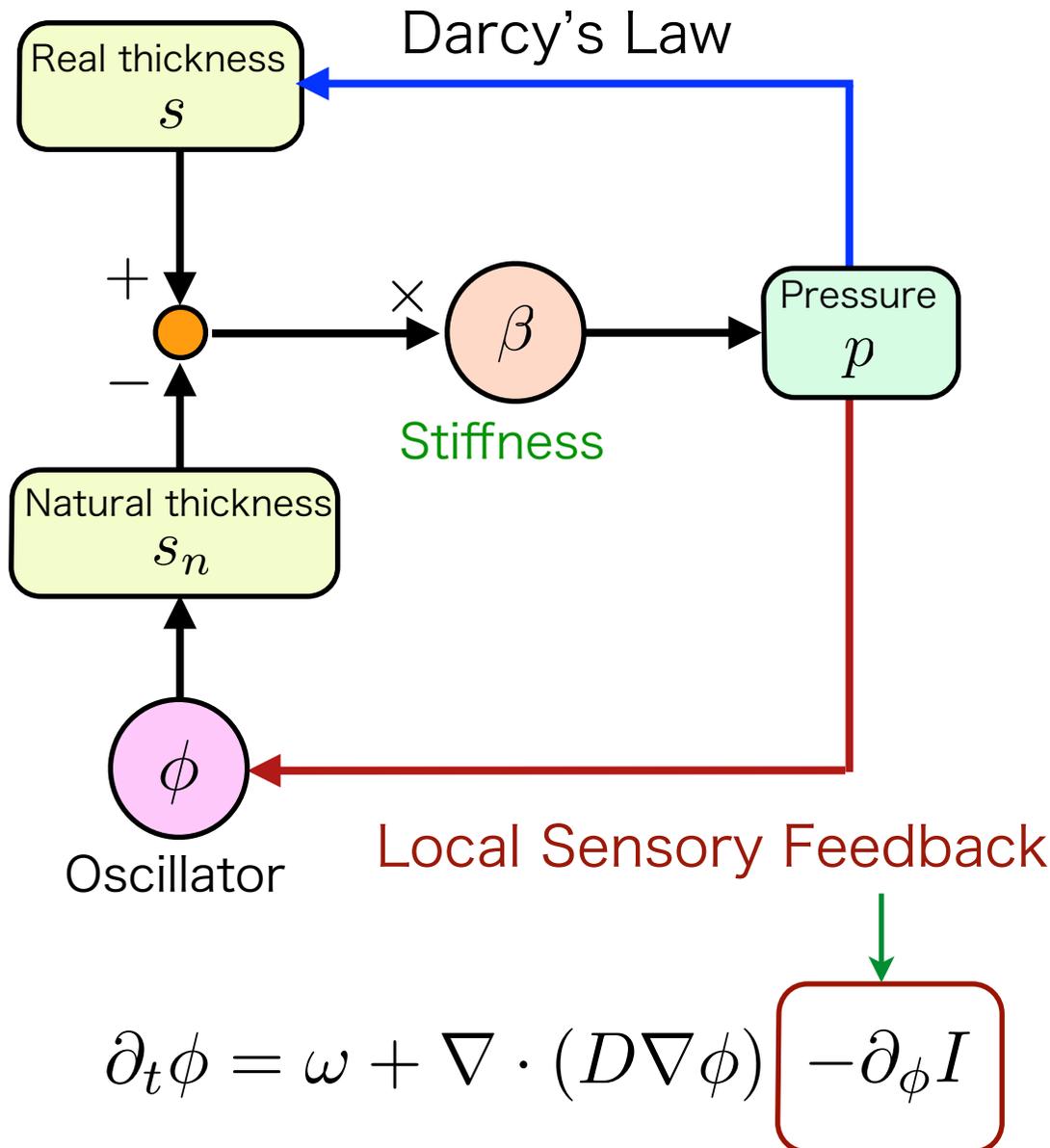


Body  Phase of oscillators



Physarum Model ver.1

Kobayashi and Nakagaki (2003)
Rediscovered by Ishiguro (2008)



Active spring whose natural length is driven by the phase oscillator ϕ

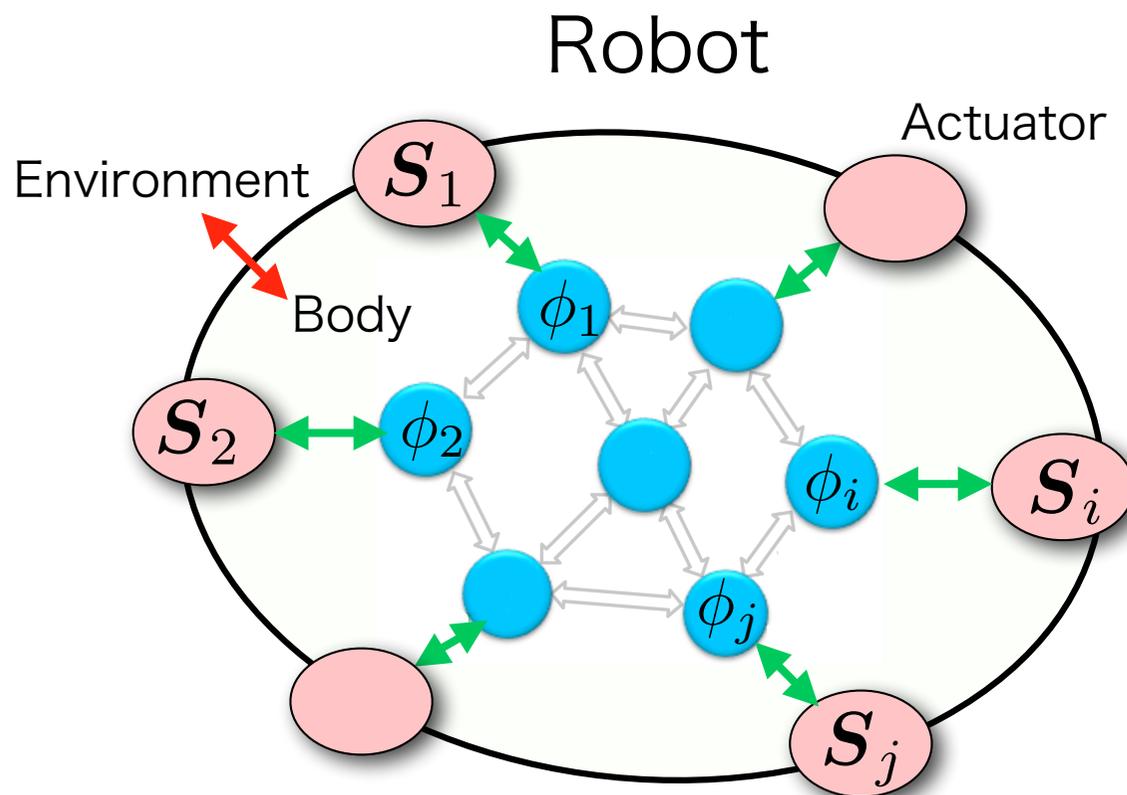
$$s_n(\phi) = \bar{s}(1 - a \cos \phi)$$

$$p = \beta(s - s_n(\phi))$$

$$\partial_t s = \nabla \cdot (sM \nabla p)$$

$$I = \frac{\sigma}{2} p^2 \quad : \text{Discrepancy Function}$$

Basic Design Scheme



ϕ_i : the i -th controller
(phase oscillator)

S_i : State variable of
the i -th actuator

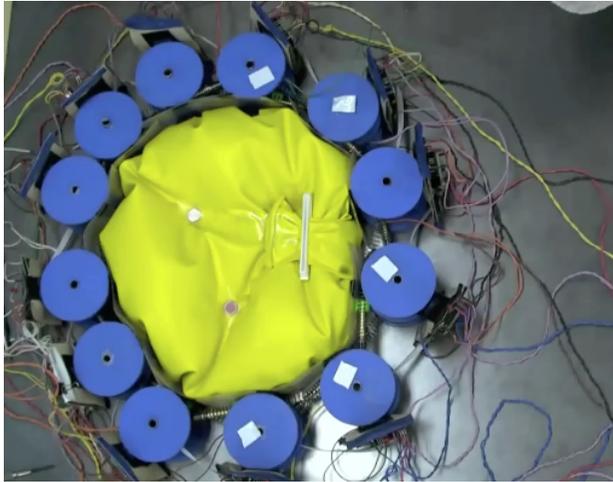
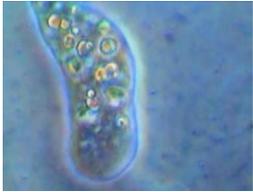
$I_i(S_i, \phi_i)$
: Frustration accumulated
in the i -th unit

→ Discrepancy Function

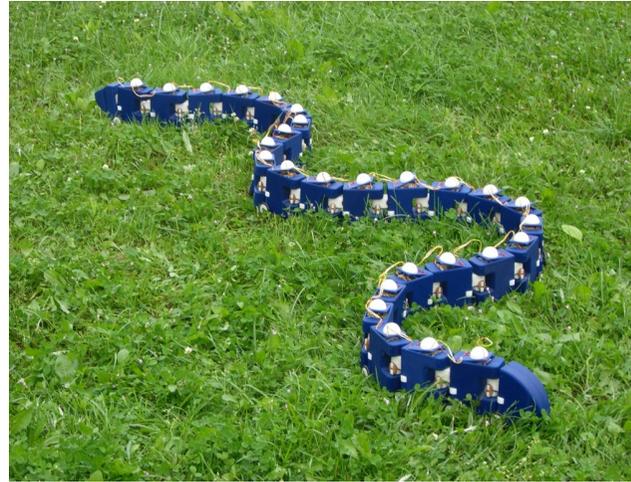
$$\partial_t \phi_i = \omega_i + \sum_j g_{ij}(\phi_i, \phi_j) - \partial_{\phi_i} I_i$$

Indirect interaction
through the body

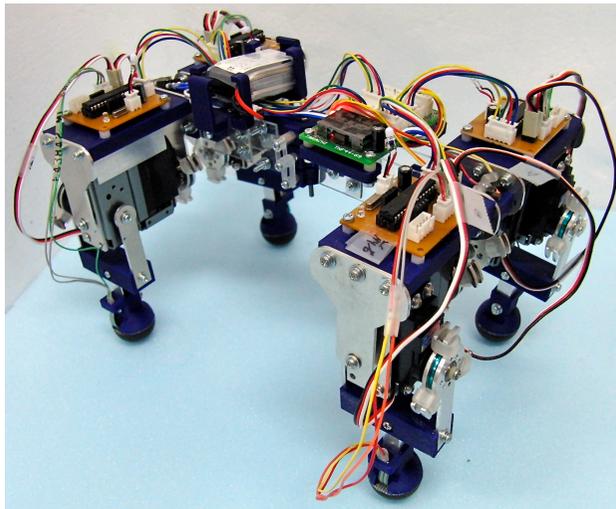
Our Robots



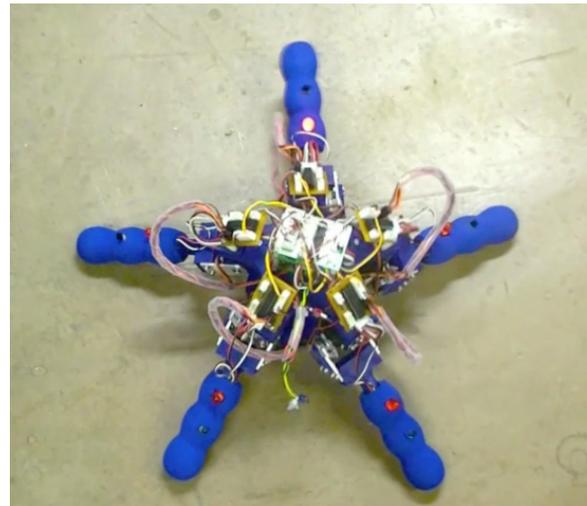
Slimy



HAUBOT



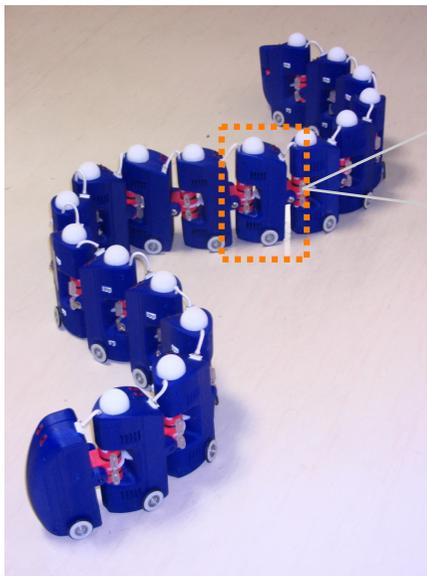
OSCILLEX



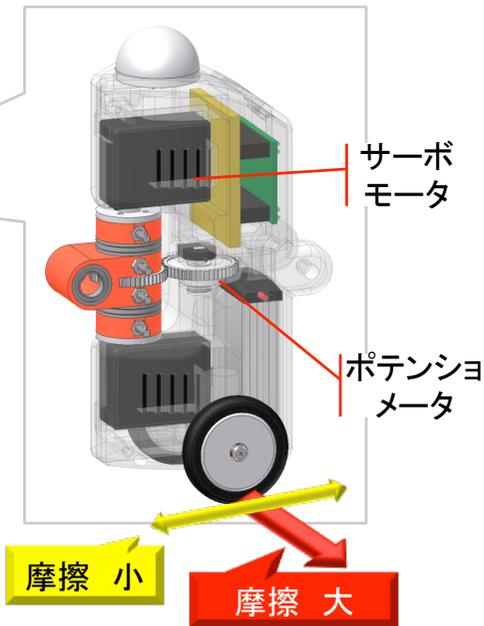
PENTABOT



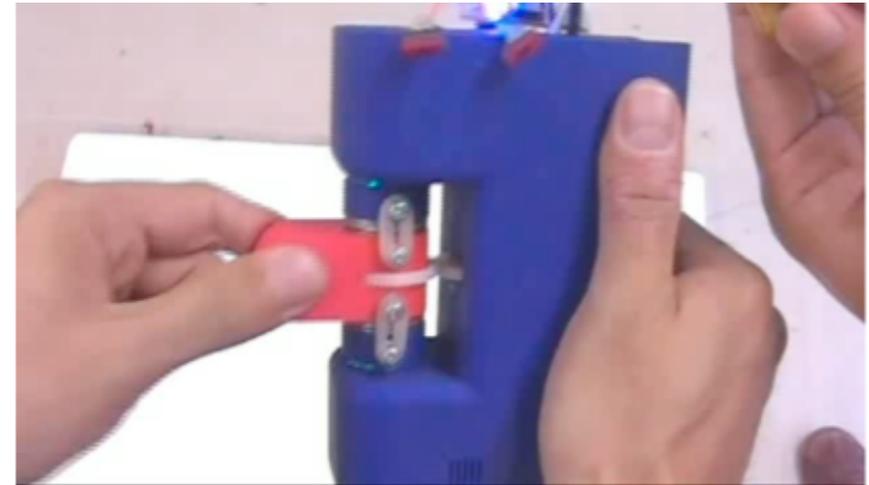
Snake Robot : HAUBOT 2



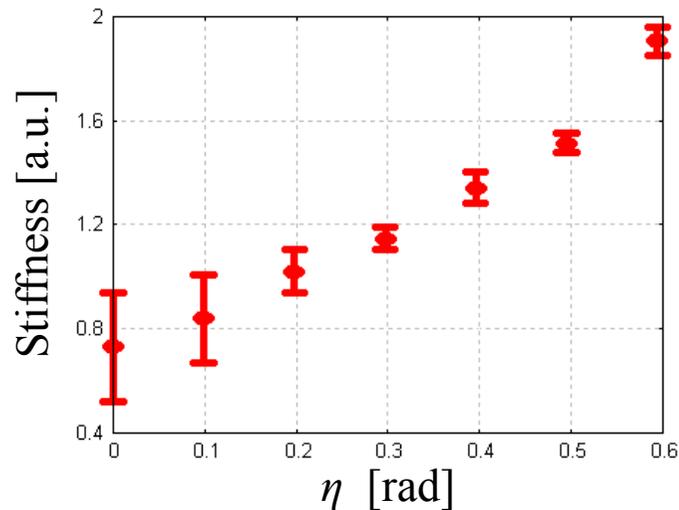
T. Sato (2011)



Joint mechanism



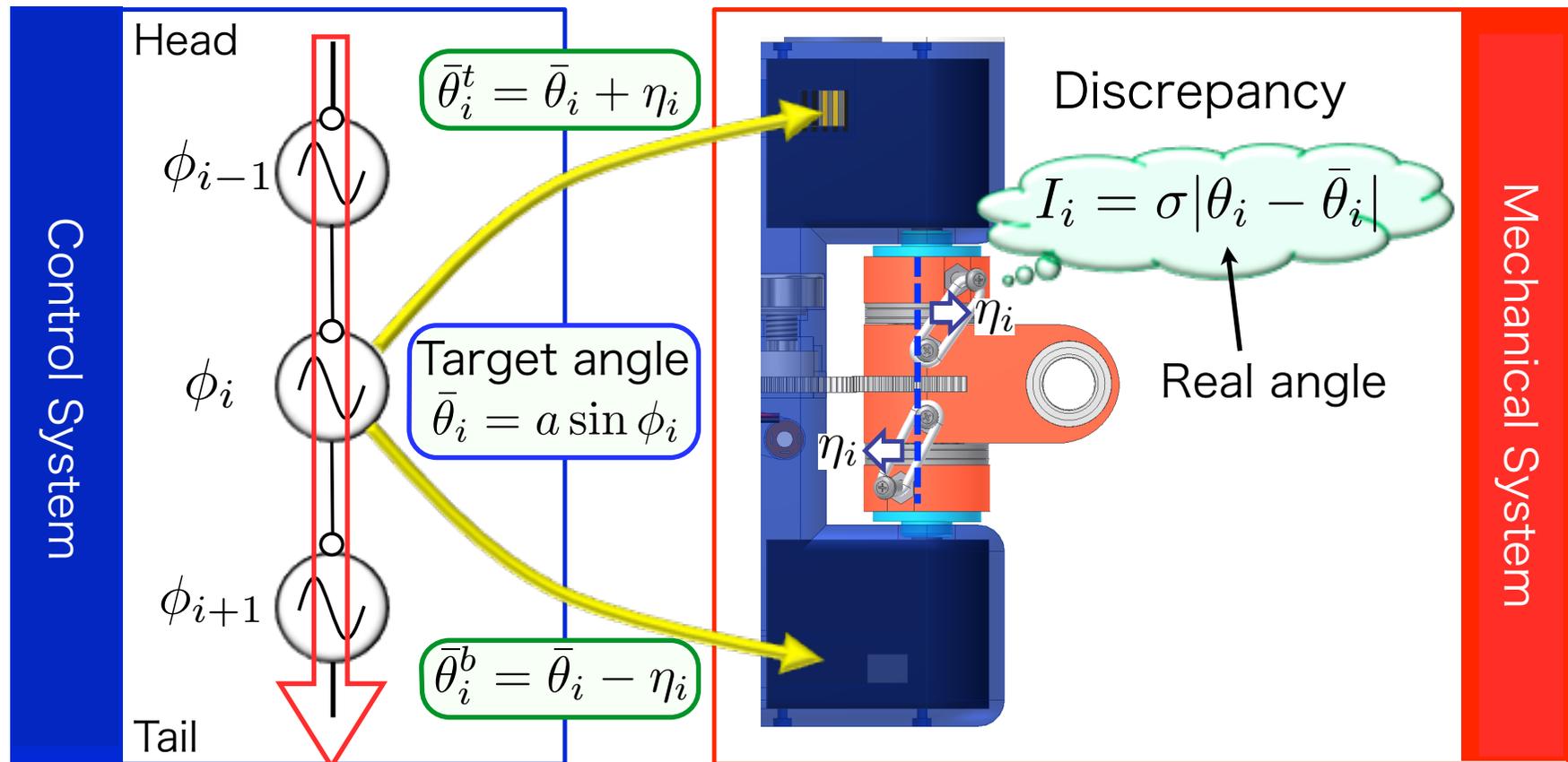
Elastic elements permit discrepancy between the motor angle (target angle) and the actual joint angle



Stiffness is also controllable by twisting

Phasic & Tonic Control

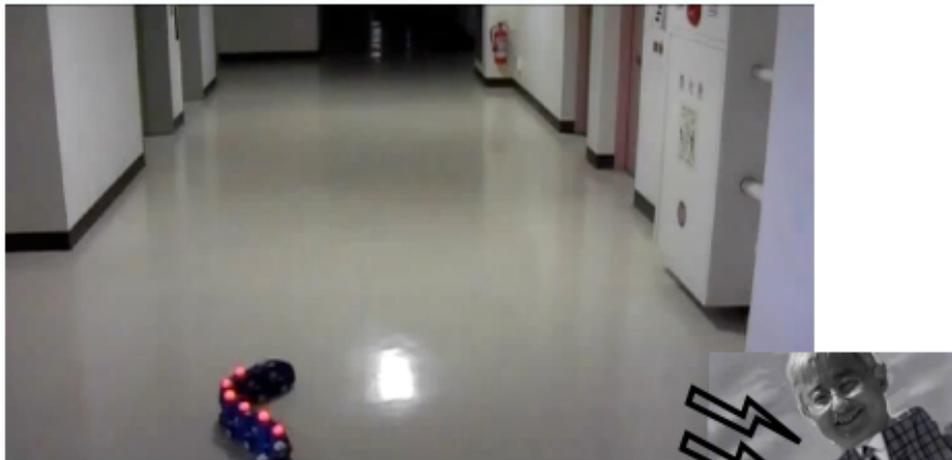
- $\partial_t \phi_i = \omega + D(\phi_{i-1} - \phi_i - \Delta\phi) - \partial_{\phi_i} I_i$
- $\partial_t \eta_i = \alpha(\beta I_i - \eta_i)$



HAUBOT 1 & 2

Phasic Control	Tonic Control
phase adjustment	stiffness adjustment
Energetic efficiency	Powerful motion

HAUBOT 1



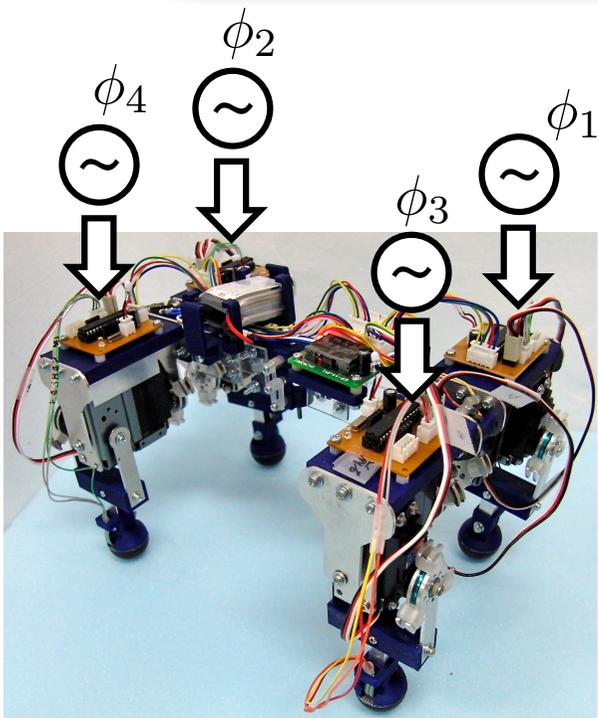
Phasic control only

HAUBOT 2



Phasic & Tonic control

OSCILLEX series



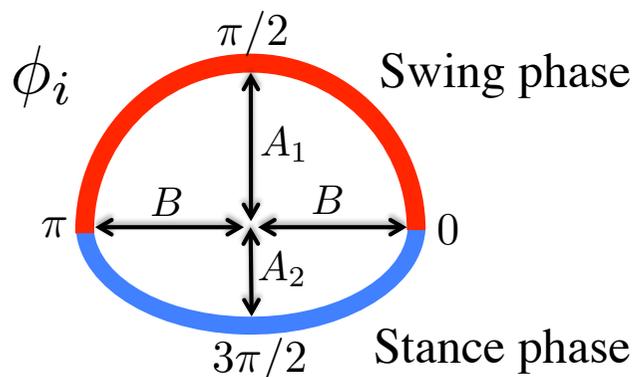
Control rule

$$\partial_t \phi_i = \omega - \sigma N_i \cos \phi_i$$

Control parameter

Load at the toe
from the center

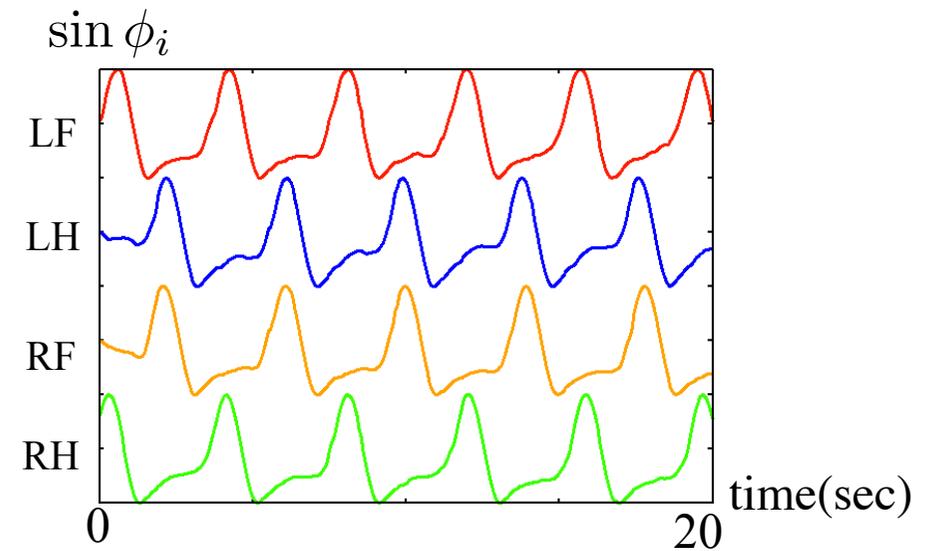
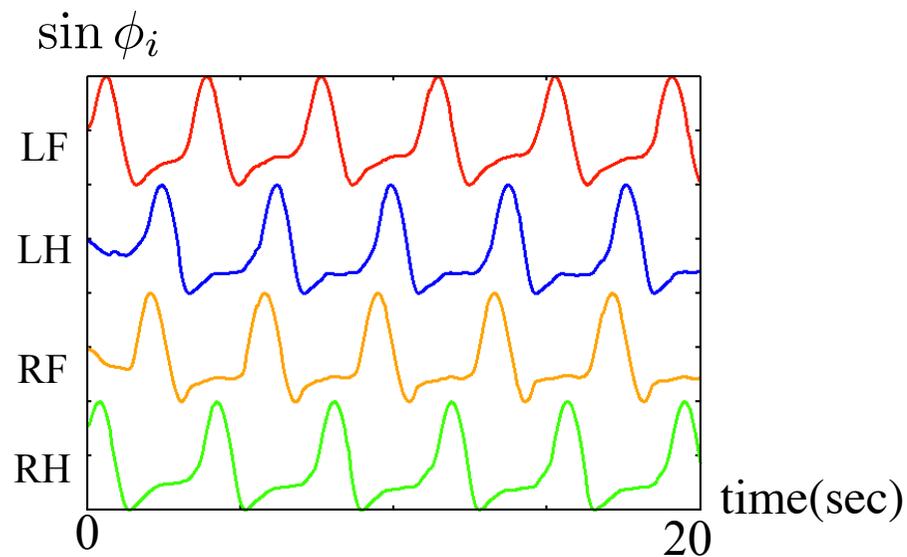
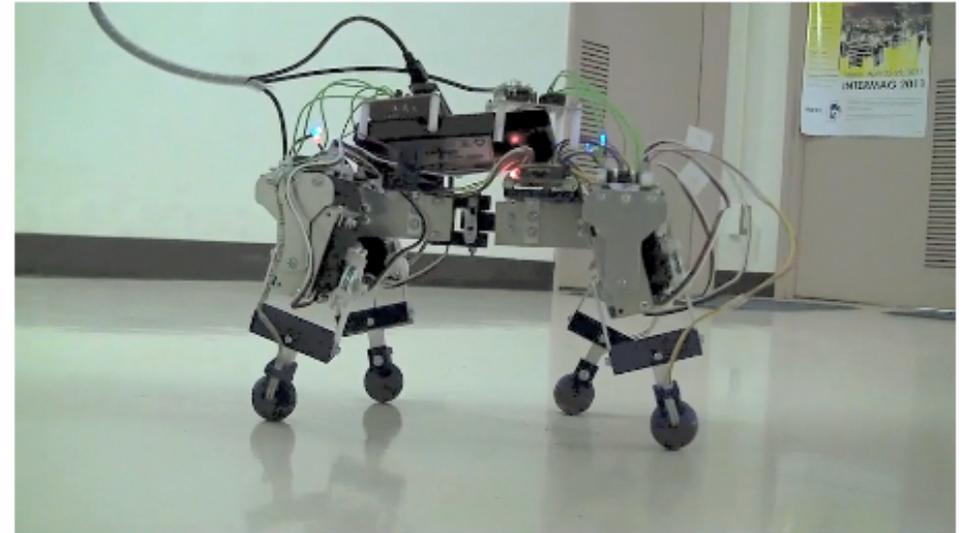
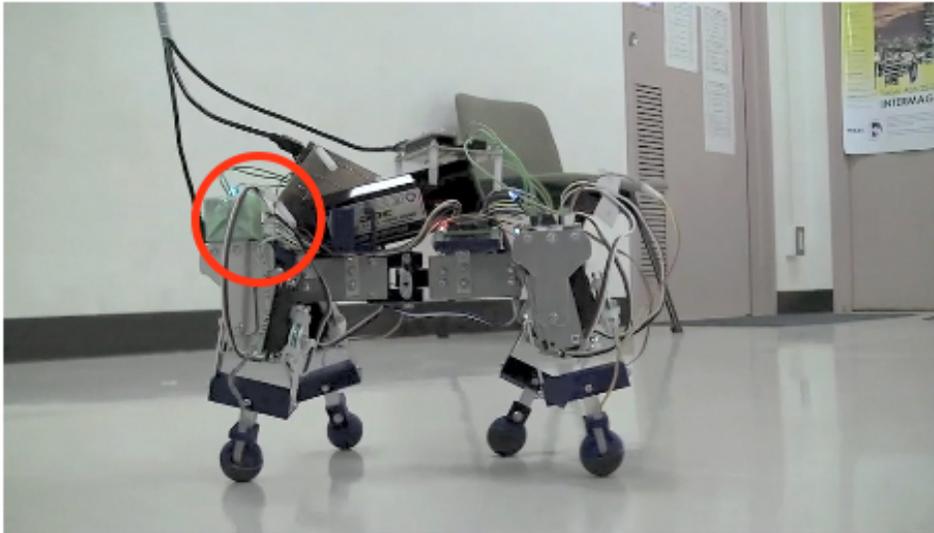
脚先位置の制御



No direct interaction between controllers, but indirect interaction through the body

Try to keep the leg in stance phase if loaded

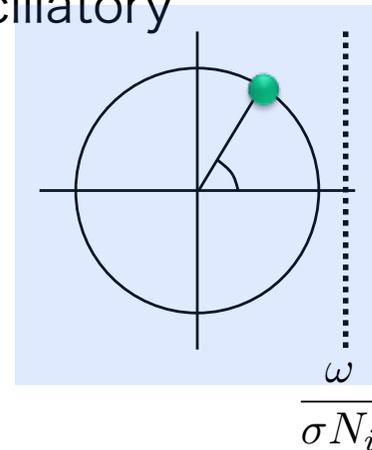
OSILLEX 1



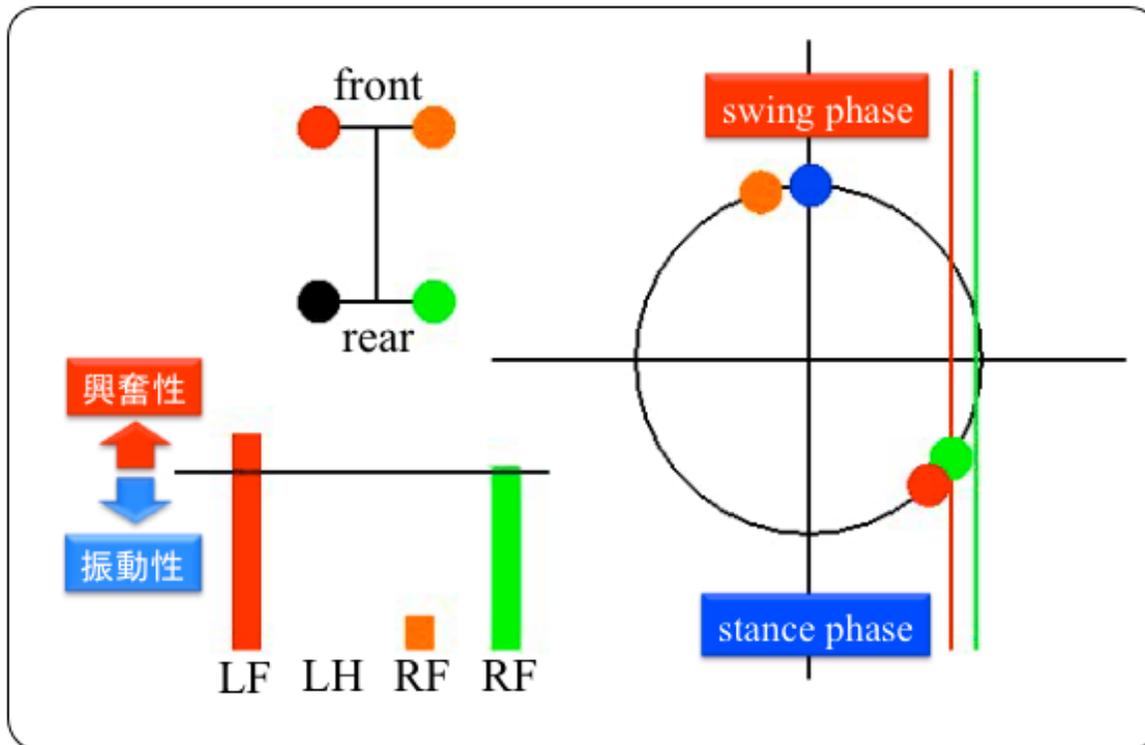
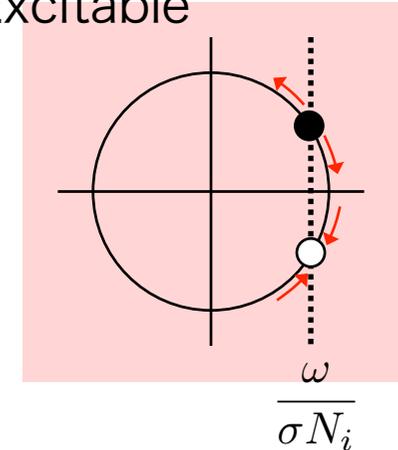
Why we call it OSILLEX ?

$$\partial_t \phi_i = \omega - \sigma N_i \cos \phi_i$$

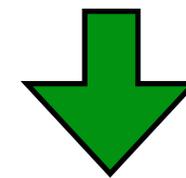
Oscillatory



Excitable

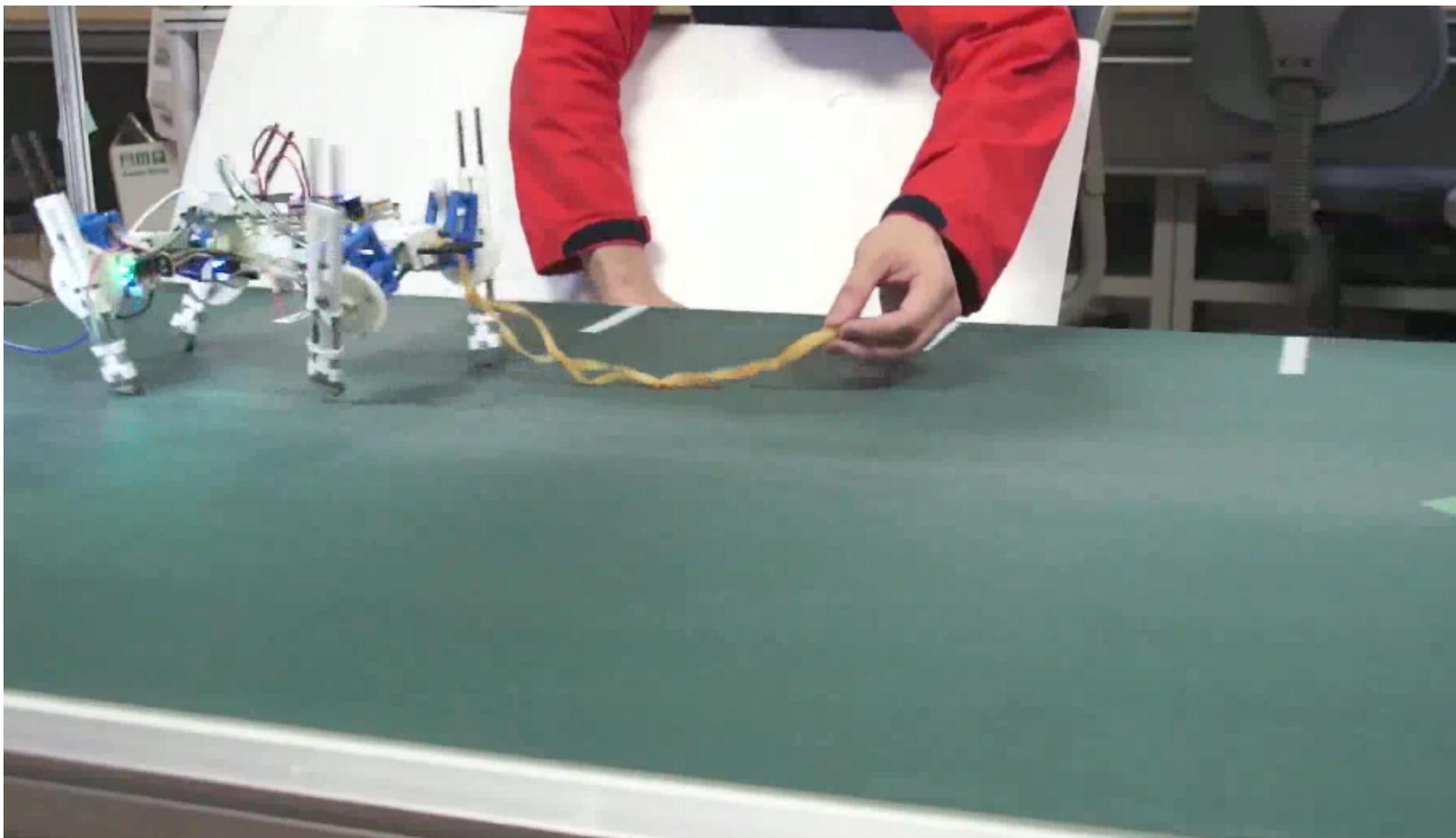


Go back and force between Oscillatory & Excitable mode



Quick transition to the stationary walking

OSCILLEX 3.1



Significance of OSCILLEX

$$\partial_t \phi_i = \omega - \sigma N_i \cos \phi_i$$

Control System

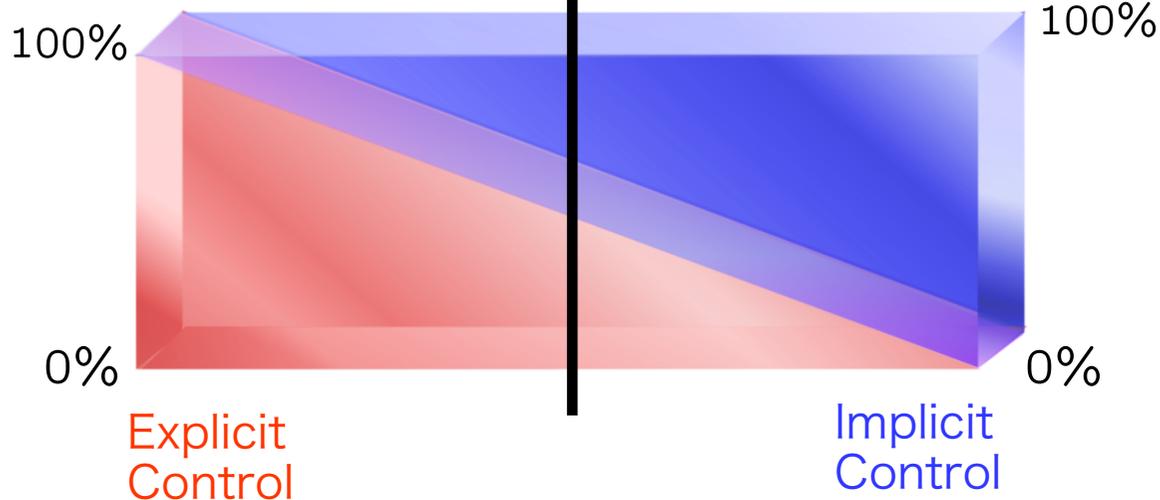


Completely Explicit Control

Brain computation

Morphological computation

Slide Bar



Body System



Completely Implicit Control

Manmalls \longleftrightarrow ? \longleftrightarrow Insects

Successful example of attaining
Adaptive Behavior by the balance of
Explicit Control and **Implicit Control**

Summary

- We extracted the concept of discrepancy function from the model of Physarum.
- The design scheme of ADC using discrepancy function was implemented to our robots, and it worked very well.
- Do not design the complicated explicit control rule.
 - Listen to the voice of the body !